

Boosted tops / jet
substructures

Michihisa Takeuchi

introduction

jet substructure

HEPTopTagger

summary

Boosted tops / jet substructures

Michihisa Takeuchi

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Blois, 1st June 2011

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HEPTopTagger

summary

introduction

top quark

- copiously produced via strong interaction at LHC
- strongly coupled with Higgs sector
- from naturalness, cancellation expected via top partner (ex. SUSY, Little Higgs)

$$\delta m_h^2 \sim \frac{3}{4\pi} y_t^2 \Lambda_{\text{SM}}^2$$


- tool for new physics search at LHC

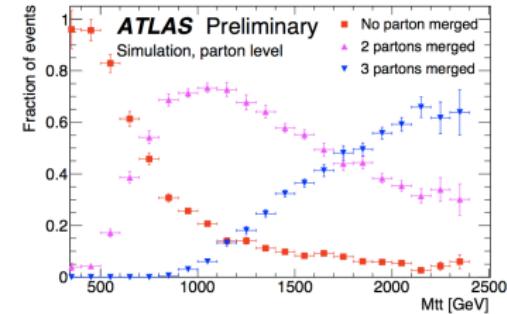
hadronic top: $t \rightarrow 3j$

- high p_T top end up a top-jet
- several top taggers available
 - looking into jet substructure
 - top \leftrightarrow QCD

[Kaplan, Rehermann, Schwartz, Tweedie] [Thaler, Wang]

[Almeida, Lee, Perez, Sterman, Sung]

- inspired by very heavy $X \rightarrow t\bar{t}$ [RS model]



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boosted particles at the LHC

1994 boosted $W \rightarrow 2$ jets from heavy Higgs [Seymour]

1994 boosted $t \rightarrow 3$ jets [Seymour]

2002 boosted $W \rightarrow 2$ jets from strongly interacting WW [Butterworth, Cox, Forshaw]

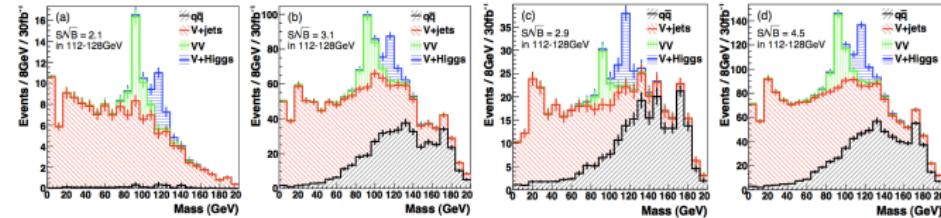
2006 boosted $t \rightarrow 3$ jets from heavy resonances [Agashe, Belyaev, Krupovnickas, Perez, Virzi]

2008 boosted $H \rightarrow b\bar{b}$ [Butterworth, Davison, Rubin, Salam]

2009 boosted $\tilde{\chi}_1^0 \rightarrow 3$ jets in R parity violating SUSY [Butterworth, Ellis, Raklev, Salam]

2009 boosted $t \rightarrow 3$ jets from top partners [Plehn, Zerwas, Spannowsky, MT]

...



$ZH(\rightarrow b\bar{b})$, $WH(\rightarrow b\bar{b})$ channel as discovery channel

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jet substructure

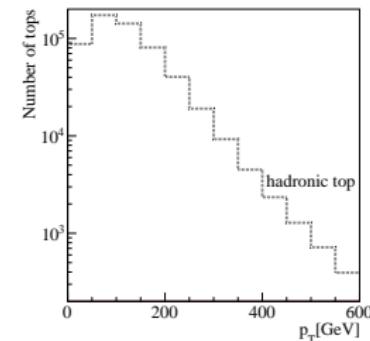
HEPTopTagger

summary

introduction

modestly boosted tops at the LHC

- top taggers are originally designed for $p_T > 500$ GeV
- not expected many in SM
- for LHC 7TeV
 - $p_T > 500$ GeV – 105fb
 - $200 < p_T < 500$ GeV – 8970fb
- need top tagger valid down to low p_T range



- light top partner (~ 500 GeV) favored to avoid little hierarchy problem
- top from the stop decay also in the range

high p_T vs. low p_T

	high p_T	↔	low p_T
source	heavy massive resonance		relatively light particles + continuum
difficulty	too collimated → difficult resolve		well separated, need large R → splash-in from UE, ISR → combinatorics

Boosted tops / jet
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plan of talk

0. introduction

1. jet substructure

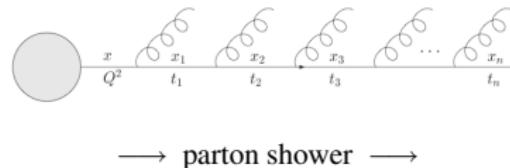
- clustering algorithm
- mass drop
- filtering

2. HEPTopTagger (Heidelberg- Eugine-Paris) – tagger for modestly boosted top

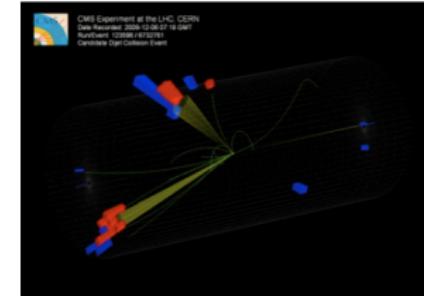
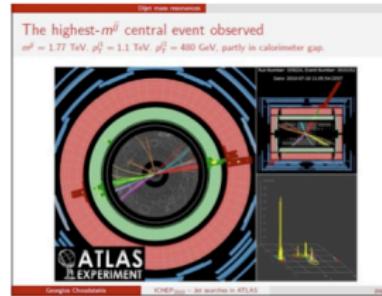
- algorithm
- efficiency & momentum reconstruction
- application to stop pairs

3. summary

- jet = collimated hadronic activity in the detector
 - well described by QCD – soft-collinear property

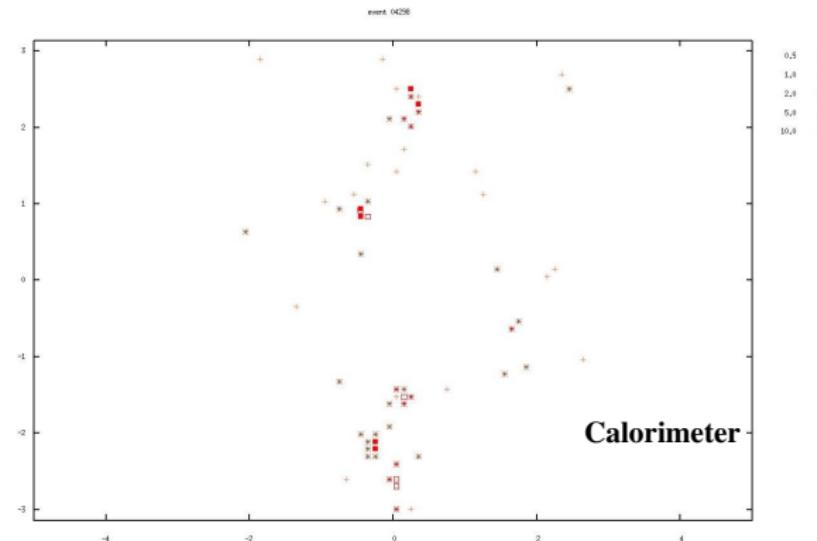
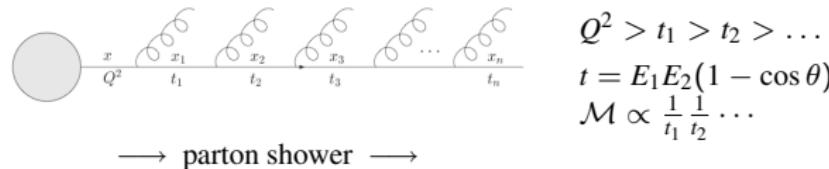


$$\begin{aligned}Q^2 &> t_1 > t_2 > \dots \\t &= E_1 E_2 (1 - \cos \theta) \\{\mathcal M} &\propto \frac{1}{t_1} \frac{1}{t_2} \dots\end{aligned}$$



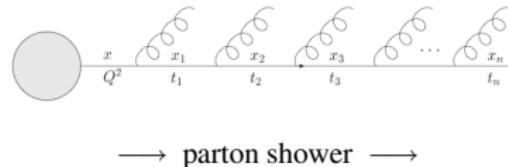
jet and QCD

- jet = collimated hadronic activity in the detector
- well described by QCD – soft-collinear property



jet and QCD

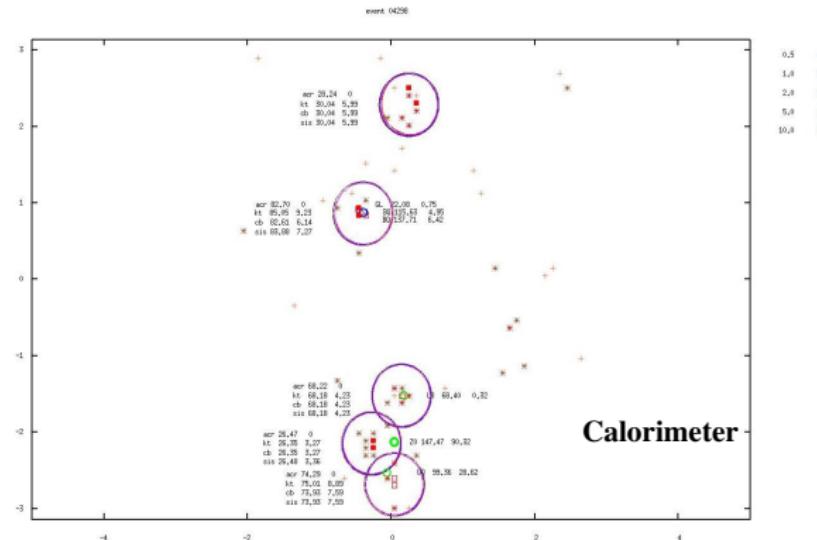
- jet = collimated hadronic activity in the detector
- well described by QCD – soft-collinear property



$$Q^2 > t_1 > t_2 > \dots$$

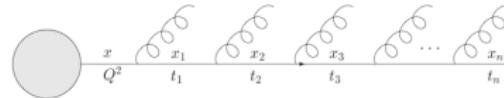
$$t = E_1 E_2 (1 - \cos \theta)$$

$$\mathcal{M} \propto \frac{1}{t_1} \frac{1}{t_2} \dots$$



clustering algorithm

- jet = collimated hadronic activity in the detector
- well described by QCD – soft-collinear property

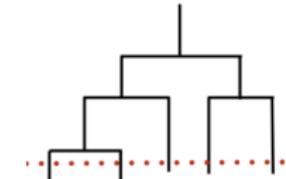


→ parton shower →
 ← clustering ←

$$\begin{aligned} Q^2 &> t_1 > t_2 > \dots \\ t &= E_1 E_2 (1 - \cos \theta) \sim E^2 \theta^2 / 2 \\ \mathcal{M} &\propto \frac{1}{t_1} \frac{1}{t_2} \dots \end{aligned}$$

clustering algorithm – sequential recombination

1. find smallest d_{ij}, d_{iB}
2. if d_{ij} , recombine ij
if d_{iB} , call i as a jet
3. repeat 1-2 until no particles left



distance measure – based on QCD (soft-collinear nature)

$$C/A \quad d_{ij} = \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = 1$$

$$kT \quad d_{ij} = \min(p_{Ti}^2, p_{Tj}^2) \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = p_T^2,$$

$$anti-kT \quad d_{ij} = \min(p_{Ti}^{-2}, p_{Tj}^{-2}) \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = p_T^{-2},$$

introduction

jet substructure

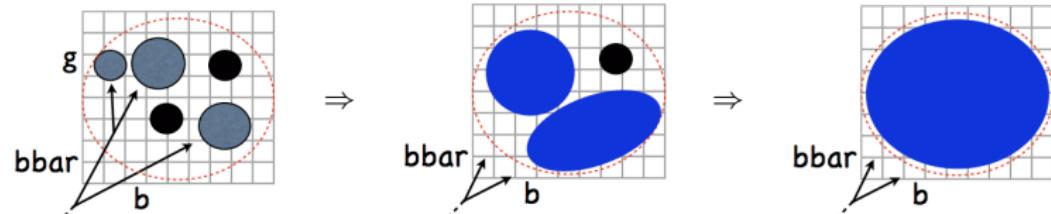
HEPTopTagger

summary

basic idea of subjet analysis

clustering

- collinear singularity of QCD → naturally collects FSR
- collects decay products from boosted object
- collects ISR and UE at the same time



introduction

jet substructure

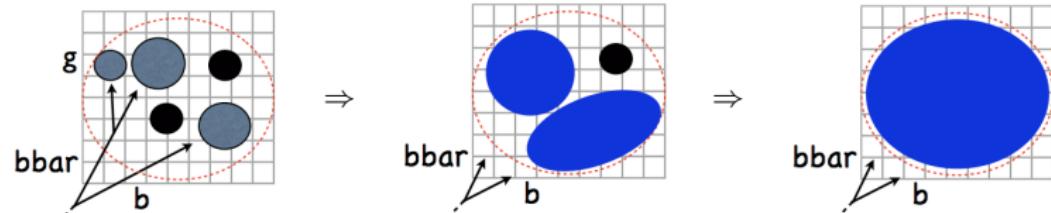
HEPTopTagger

summary

basic idea of subjet analysis

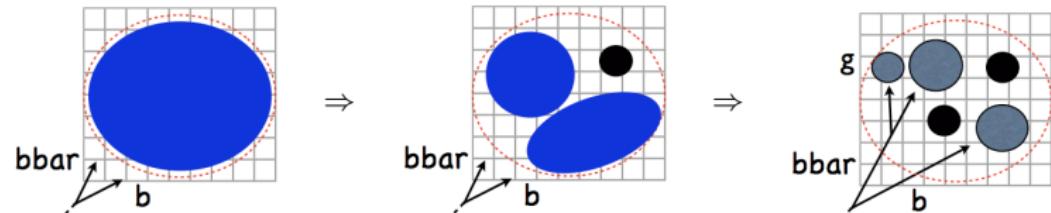
clustering

- collinear singularity of QCD → naturally collects FSR
- collects decay products from boosted object
- collects ISR and UE at the same time



undoing clustering

- no soft-collinear singularity for decay of boosted object → mass drop, p_T drop
- $$j = j_1 + j_2, \quad m_j \gg m_{j_1}, m_{j_2} \text{ (massive particle)} \leftrightarrow m_j \sim m_{j_1} \gg m_{j_2} \text{ (QCD)}$$
- want collect FSR but reject ISR and UE



introduction

jet substructure

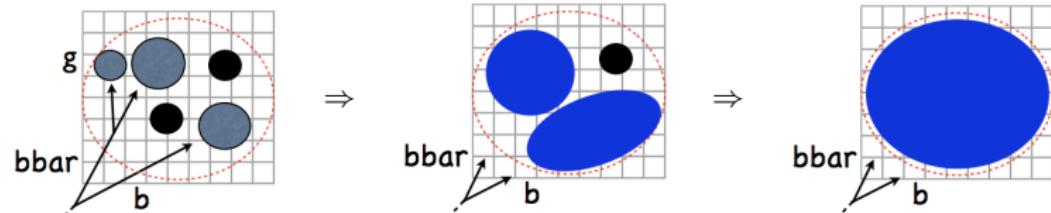
HEPTopTagger

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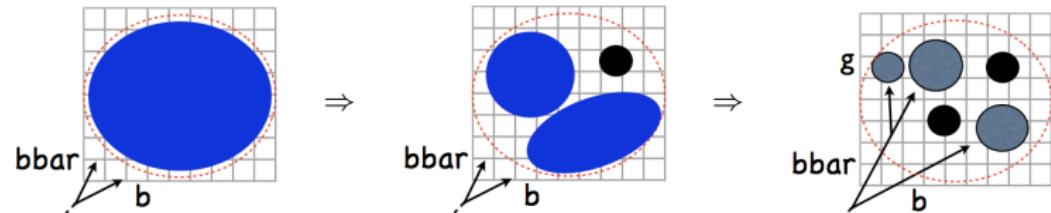
clustering

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- want collect FSR but reject ISR and UE → need filtering



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jet substructure

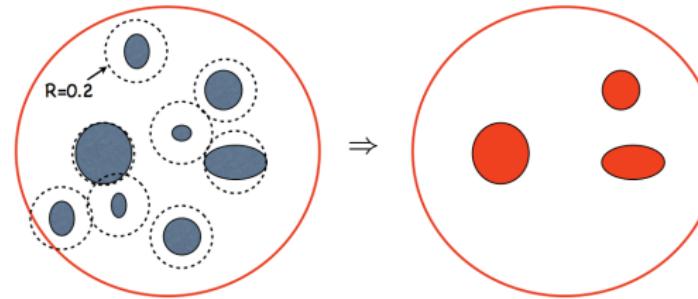
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summary

jet filtering

jet filtering [Butterworth et al.]

- take a jet defined with R , for example $R = 1.0$
- recombine the constituents with smaller R_{filt} , for example $R_{\text{filt}} = 0.2$
- take only first hardest n_{filt} subjets (discard others)



- R_{filt} and n_{filt} : tunable parameter ← depends on what want to tag
- $H \rightarrow b\bar{b}$, take 3 hardest subjets (for 1 gluon radiation $H \rightarrow b\bar{b}g$)
- $t \rightarrow bjj$, take 5 hardest subjets (for 2 gluon radiation $t \rightarrow bg(jjg)$)

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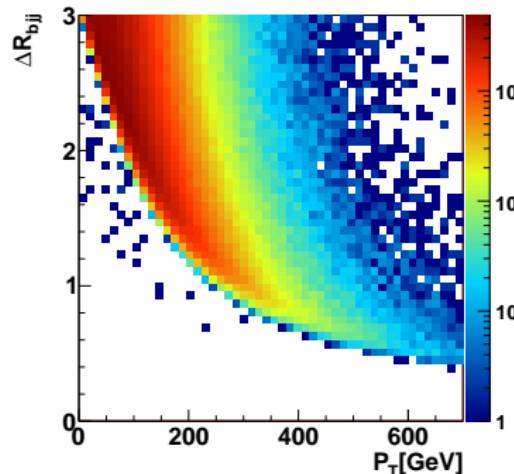
jet substructure

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summary

fat jets

- focus on low p_T tops with heavy m_t
 - decay products well separated, need large R
- $R = 1.5$ to have top with $p_T \sim 200$ GeV



- valid seamlessly from low p_T to high p_T

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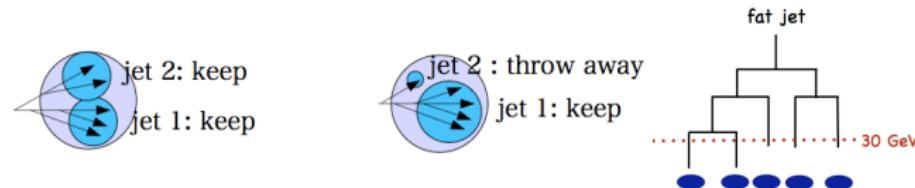
jet substructure

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summary

1. fat jets – C/A($R = 1.5$), $p_T^{\text{fatjet}} > 200 \text{ GeV}$ **2. mass drop criterion**

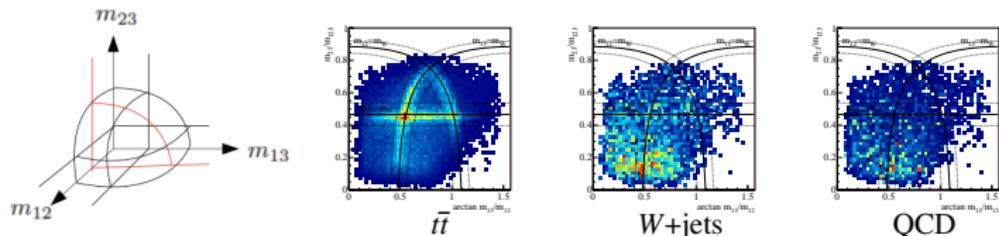
- find hard proto-jets $m_j < 30 \text{ GeV}$, $m_{j1} < 0.8m_j$ to keep j_1 and j_2

**3. choose 3 hard proto-jets with best filtered mass**

- $|m_{jjj}^{\text{filt}} - m_t| < 25 \text{ GeV}$ and $p_T^{\text{rec}} > 200 \text{ GeV} \rightarrow \text{top candidate}$

4. check mass ratios

- m_t condition: $m_t^2 = m_{123}^2 = m_{12}^2 + m_{13}^2 + m_{23}^2 \rightarrow$ spherical surface: 2D mass ratios



- W mass condition, soft-collinear cut \rightarrow **tagged top**

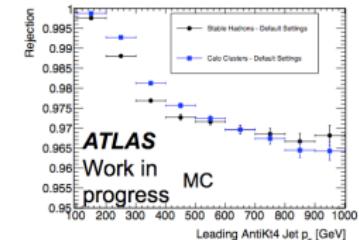
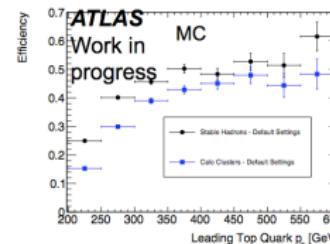
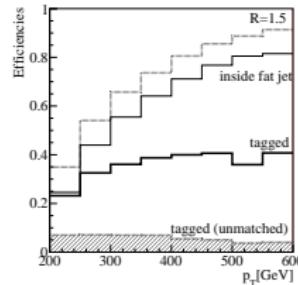
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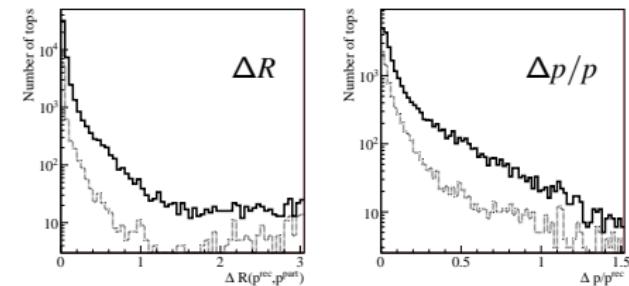
efficiency



- efficiency $\sim 35\%$ for hadronic tops, $2 \sim 4\%$ mis-tag rate
- validation with ATLAS experimentalists in Heidelberg

momentum reconstruction

- momentum well reconstructed
- better reconstruction for larger p_T
 - solid: $p_T^{\text{rec}} > 200\text{GeV}$
 - dotted: $p_T^{\text{rec}} > 300\text{GeV}$



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jet substructure

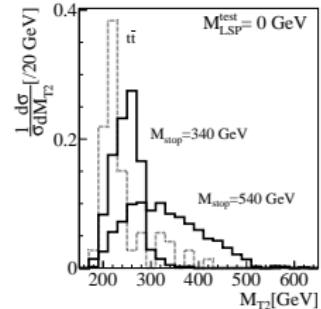
HEPTopTagger

summary

stop pairs

hadronic $\tilde{t}\tilde{t}^*$ [T. Plehn, M. Spannowsky, MT, D. Zerwas]

- $m_{\tilde{\chi}_1^0} = 98 \text{ GeV}, \tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$ (100%)
- main BG: $t\bar{t}$ +jets, W +jets and QCD (*Alpgen-Pythia*)
- set of cuts
 - no lepton, $\cancel{E}_T > 150 \text{ GeV}$
 - 2 tagged tops with $p_T^{\text{rec}} > 200/200 \text{ GeV} \rightarrow W+\text{jets}, Z+\text{jets}$ negligible
 - *b*-tag for 1st tagged top \rightarrow QCD negligible
 - $m_{T2} > 250 \text{ GeV} \rightarrow$ reduce $t\bar{t}$



events in 1 fb^{-1}	$\tilde{t}_1\tilde{t}_1^*$		$t\bar{t}$	QCD	$W+\text{jets}$	$Z+\text{jets}$	S/B	$S/\sqrt{B} \text{ fb}^{-1}$
$m_{\tilde{t}} [\text{ GeV}]$	340	390	440	490	540	640		340
$p_{T,j} > 200 \text{ GeV}, \ell \text{ veto}$	728	447	292	187	124	46	$87850 \cdot 2.4 \cdot 10^7$	$1.6 \cdot 10^5$
$\cancel{E}_T > 150 \text{ GeV}$	283	234	184	133	93	35	$2245 \cdot 2.4 \cdot 10^5$	1710
first top tag	100	91	75	57	42	15	743	2240
second top tag	15	12.4	11	8.4	6.3	2.3	7590	90
<i>b</i> tag	8.7	7.4	6.3	5.0	3.8	1.4	114	1.2 $\cdot 10^{-2}$
$m_{T2} > 250 \text{ GeV}$	4.3	5.0	4.9	4.2	3.2	1.2	32	1.2 $\cdot 10^{-5}$
							19	8.3 $\cdot 10^{-2}$
							4.2	0.40
							$\lesssim 0.6$	5.9
							$\lesssim 0.2$	0.88
							$\lesssim 0.1$	6.1
							$\lesssim 0.05$	
							$\lesssim 0.03$	

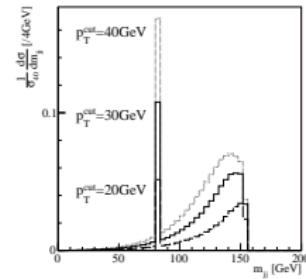
– $S/B \sim 1, S/\sqrt{B} > 5 \text{ for } 10 \text{ fb}^{-1}$

- stop mass from $m_{T2}(m_{\tilde{\chi}_1^0})$ endpoint [C. G. Lester, D. J. Summers] [like sleptons or sbottoms]

stop pairs

semileptonic $\tilde{t}_1 \tilde{t}_1^* \rightarrow (b\ell\nu \tilde{\chi}_1^0) (\bar{b}j j \tilde{\chi}_1^0)$ [arXiv:1102.0557 [hep-ph] T. Plehn, M. Spannowsky, MT]

1. exactly one lepton ($p_T > 20$ GeV, $|\eta| < 2.5$)
2. $\cancel{E}_T > 150$ GeV
3. one tagged hadronic top
(HEPTOPTAGGER, $p_T > 200$ GeV)
4. one b tag among the leading 3 jets outside the tagged top
($p_T > 25$ GeV, $|\eta| < 2.5$)
5. $m_{b\ell} < \sqrt{m_t^2 - m_W^2} = 154.6$ GeV. [cf. CDF m_{jj} by tops (arXiv:1104.4087 T. Plehn, MT)]



	$\tilde{t}_1 \tilde{t}_1^*$				$t\bar{t}$	$W+\text{jets}$	S/B	$S/\sqrt{B}_{20\text{fb}^{-1}}$
$m_{\tilde{t}} [\text{GeV}]$	340	440	540	640			440	440
0. cross section	5090	1280	402	146	$9.2 \cdot 10^5$	$2.1 \cdot 10^5$	0.001	3.8
1. one lepton	1471	373	118	42.5	$2.6 \cdot 10^5$	$1.3 \cdot 10^5$	0.001	2.7
2. $\cancel{E}_T > 150$ GeV	569	239	90.2	35.5	9825	4512	0.017	8.9
3. hadronic top tag	74.5	38.0	16.8	7.72	1657	141	0.021	4.0
4. tagged b jet	31.2	15.9	7.33	3.38	668	4.35	0.024	2.7
5. $m_{b\ell} < m_{b\ell}^{\max}$	27.5	13.7	6.34	2.90	642	2.61	0.021	2.4

– cut basis method:

- use $\cancel{E}_T = p_{\nu,T}$
- check solution for $p_{\nu,z}$
- not promising $S/B \sim 0.1, S/\sqrt{B}_{10 \text{ fb}^{-1}} \sim 2.2$
- not reasonable with additional \cancel{E}_T sources.

→ our approach:

- reconstruct top momentum
- compare with \cancel{E}_T

introduction

jet substructure

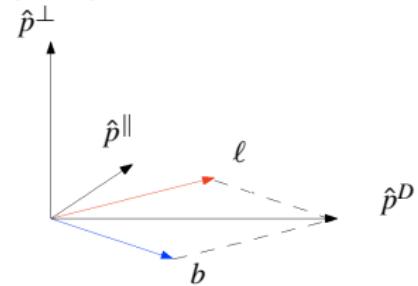
HEPTopTagger

summary

only 3 observable in lab. frame

$$E_\ell, \quad E_b, \quad m_{b\ell} \text{ (equivalent to } \theta_{bl})$$

$$\vec{p}_\nu = x_D \hat{p}^D + x_{||} \hat{p}^{||} + x_{\perp} \hat{p}^{\perp}$$



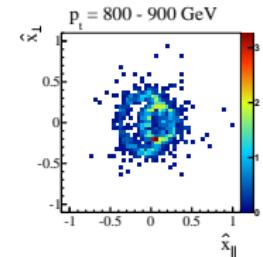
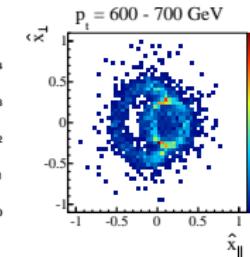
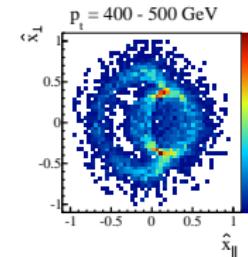
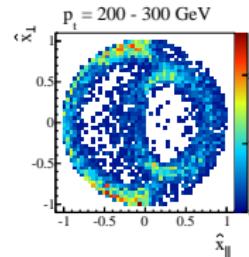
2 constraints

$$(p_\ell + p_b + p_\nu)^2 = m_t^2, \quad (p_\ell + p_\nu)^2 = m_W^2.$$

one additional assumption needed to solve

orthogonal approximation

- $x_{||} = 0$

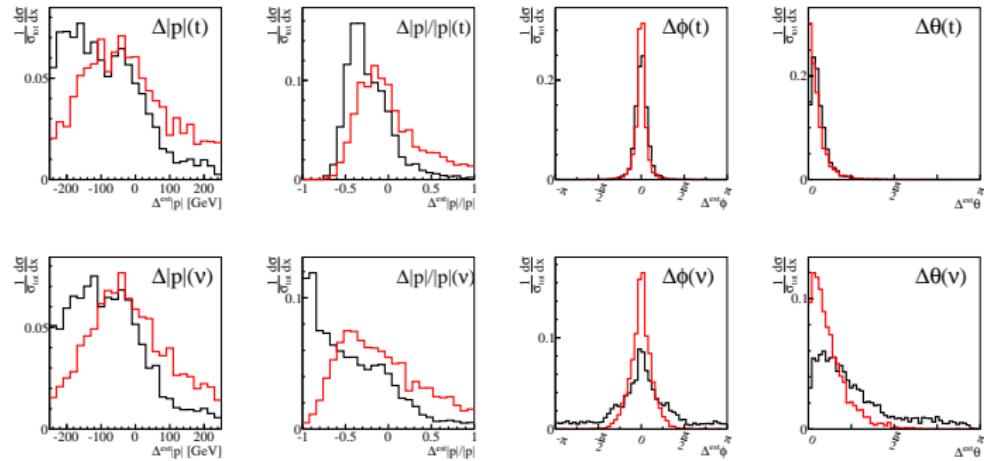


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summary

momentum reconstruction ($\cancel{E}_T > 200\text{GeV}$)

- red: orthogonal approx. black: decay plane approx.
- $\Delta|p|(t) = |p_{\text{top}}^{\text{rec}}| - |p_{\text{top}}^{\text{parton}}|$, $\Delta|p|(\nu) = |p_{\nu}^{\text{rec}}| - |p_{\nu}^{\text{parton}}|$
- better top momentum reconstruction (compared with ν)
- in particular, good ϕ reconstruction.

introduction

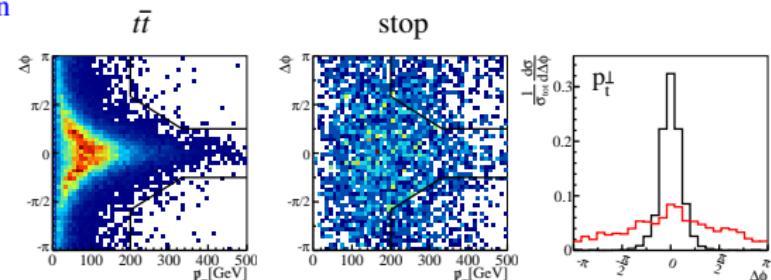
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summary

 ϕ_{top} vs. \cancel{E}_T correlation

$$\Delta\phi_{\text{top}} = \phi_{\text{top}}^{\text{rec}} - \phi(\cancel{E}_T)$$



for events with large \cancel{E}_T , top direction and neutrino direction is aligned.

$$|\Delta\phi| > \frac{13}{12}\pi - \frac{\cancel{E}_T}{400 \text{ GeV}}\pi \quad \cancel{E}_T > 200 \text{ GeV} \quad |\Delta\phi| > \frac{\pi}{4}.$$

	orthogonal approximation				S/B	decay plane approximation				S/B
	$\tilde{t}_1 \tilde{t}_1^*$	$t\bar{t}$	$W+\text{jets}$	S/B		$\tilde{t}_1 \tilde{t}_1^*$	$t\bar{t}$	$W+\text{jets}$	S/B	
$m_{\tilde{t}} [\text{GeV}]$	340	440	540	640	440	340	440	540	640	440
1.-5. base cuts	27.38	13.71	6.33	2.89	642.72	2.63	0.021			
6. approximation	14.81	7.69	3.61	1.66	285.16	1.41	0.027	27.33	13.67	6.31
7. $p_T^{\text{est}} > 200 \text{ GeV}$	8.61	4.53	2.41	1.24	215.62	0.60	0.021	9.13	5.16	2.87
8. \cancel{E}_T vs. $\Delta\phi$ cut	0.97	1.52	1.23	0.76	0.72	0.02	2.06	1.22	1.82	1.53
								1.02	1.02	1.02
								1.31	0.06	1.33

$$- \boxed{S/B \sim 2, S/\sqrt{B}_{10\text{fb}^{-1}} \sim 5} \quad (\text{cut basis: } S/B \sim 0.1, S/\sqrt{B}_{10\text{fb}^{-1}} \sim 2.2)$$

- top – closest to new physics
- jet substructure
 - distinguish boosted object and QCD
 - mass drop
 - filetring
- HEPTopTagger: (**Heidelberg-Eugine-Paris**)
 - focus on low p_T tops ($p_T > 200\text{GeV}$)
 - fat jets kill combinatorics
 - efficiency: top $\sim 35\%$, mis-tag rate W+jets: 4%, QCD: 2%
 - hadronic top momentum well reconstructed
 - leptonic top direction well reconstructed
 - stop pairs: hadronic channel: $S/B \sim 1, S/\sqrt{B} > 5$ for 10fb^{-1}
semi-leptonic channel: $S/B \sim 2, S/\sqrt{B} > 5$ for 10fb^{-1}

code available on

<http://www.thphys.uni-heidelberg.de/~plehn/heptoptagger/index.html>